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# THE EPR SPECTRA OF TETRADENTATE SCHIFF BASE COMPLEXES OF COPPER (II) IV. $\mathbf{N}, \mathbf{N}$-bis-(pyrrole-2-aldehyde)ethylenediimine 

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#### Abstract

The EPR spectrum of $\mathrm{N}, \mathrm{N}^{\prime}$-bis-(pyrrole-2-aldehyde)ethylenediimino $\mathrm{Cu}(\mathrm{II}),[\mathrm{Cu} \text { en(pyal) })_{2}$ ] has been investigated in a doped singie crystal of the corresponding nickel (II) chelate. The imine and pyrrole nitrogens were found to be chemically inequivalent thus giving rise to unequal coupling constants. The parameters in the doublet spin- Hamiltonian are found to be: $g_{z}=2.168 \pm 0.001, g_{x}=2.042 \pm 0.002, g_{y}=2.043 \pm 0.002, A_{z}^{\mathrm{Cu}}=197.5 \times 10^{-4} \mathrm{~cm}^{-1}$, $A_{x}^{\mathrm{Cu}}=28.5 \times 10^{-4} \mathrm{~cm}^{-1}, A_{y}^{\mathrm{Cu}}=27.3 \times 10^{-4} \mathrm{~cm}^{-1}$, imine $A_{z}^{N}=14.1 \times 10^{-4} \mathrm{~cm}^{-1}, A_{x}^{N}=A_{y}^{N}=15.5 \times 10^{-4} \mathrm{~cm}^{-1}$, pyrrole $A_{z}^{N}=17.7 \times 10^{-4} \mathrm{~cm}^{-1}, A_{x}^{N}=A_{y}^{N}=15.5 \times 10^{-4} \mathrm{~cm}^{-1}$, methine $A_{z}^{H}=7.0 \times 10^{-4} \mathrm{~cm}^{-1}$, $A_{x}^{H}=A A_{y}^{H}=8.2 \times 10^{-4} \mathrm{~cm}^{-1}$. These parameters are related to the coefficients of the molecular orbital containing the unpaired electron. Preliminary crystal data for the nickel chelate are also given.


## KEY WORDS

EPR spectrum, $\mathrm{N}^{\prime} \mathrm{N}^{\prime}$-bis-(pyrrole-2-aldehyede)ethylenediimino $\mathrm{Cu}(\mathrm{II})$, magnetic parameters, molecular orbitals, ligand field, crystal data.

## INTRODUCTION

Transition metal complexes of tetradentate ligands resulting from the $2: 1$ condensation of salicylaldehyde or $\beta$-diketones with diamines have been the subject of many investigations. ${ }^{1-5}$ These ligands form planar, neutral complexes of the cis " $\mathrm{N}_{2} \mathrm{O}_{2}$ " type and furnish fields whose approximate symmetry is described by the $C_{2 v}$ point group. The related tetradentate Schiff base complexes of the " $\mathrm{N}_{4}$ " type have been somewhat ignored. Only recently have complexes derived from o-aminobenzaldehyde been investigated in any detail. ${ }^{6-8}$ There is even a greater dearth of information concerning tetradentate complexes derived from pyrrole-2-aldehyde. This is surprising since they contain the biologically important pyrrole moiety and their ability to form single crystals far exceeds that of the phthalocyanines and the porphyrins.

The condensation product of two moles of

[^0]pyrrole-2-aldehyde and one mole of ethylenediamine and its complexes of copper(II) and nickel(II) were first reported by Pfieffer ${ }^{9}$ et al. and later studied in greater detail by Weber and Clarke ${ }^{10,11}$ but no EPR data have been presented. Stackelberg ${ }^{12}$ attempted to obtain crystal data for the copper complex but his analysis is incomplete. The purpose of this study is to investigate the copper complex by EPR spectroscopy. To obtain the maximum amount of bonding information, this study was carried out on a magnetically dilute sample in order to eliminate dipolar broadening thus enabling the resolution of hyperfine and superhyperfine structure in the spectrum. This was accomplished by doping small amounts of the paramagnetic copper complex into a crystal of the diamagnetic nickel complex.

## EXPERIMENTAL

The ligand and the nickel chelate were prepared as described in the literature. ${ }^{9}$ Small amounts of $\mathrm{Cu}(\mathrm{II})$ were added during the synthesis of the $\mathrm{Ni}(\mathrm{II})$ complex


FIGURE 1 Molecular geometry of the complexes where $\mathrm{M}=\mathrm{Ni}(\mathrm{II}), \mathrm{Cu}(\mathrm{II})$.
to form the doped compound. Isotopically pure ( $99.87 \%$ ) ${ }^{63} \mathrm{Cu}($ II $)$, as the nitrate, was used in doping to reduce the complexity of the hyperfine splitting. Single crystals of the pure nickel chelate were used to collect x-ray data while Cu-doped ( $1-3 \%$ ) crystals of the nickel chelate were used for EPR studies.

The EPR spectrometer and the associated equipment have been previously described. ${ }^{13}$ The spectral analysis was simplified by the use of simulated spectra calculated on a Nicolet Nic-80 computer by means of the program "EPRCAL". The data reduction procedure described by Billings and Hathaway ${ }^{14}$ employed in our previous studies was modified for use in the present case because we could obtain data in only two orthogonal planes. Since the largest $g$-value $\left(g_{z}\right)$, obtained from the powdered crystal spectra was observed in one single crystal plane, their method could be modified to accommodate the present system. The modification we have employed is described in the appendix.

Translucent orange crystals of $\mathrm{Ni}\left[\mathrm{en}(\text { pyal })_{2}\right]$ elongated along the a-axis were obtained by slow evaporation of a chloroform solution. Found: $\mathrm{C}-53.28 \%, \mathrm{H}-4.51 \%, \mathrm{~N}-21.10 \%$; Calc: $\mathrm{C}-53.18 \%$, $\mathrm{H}-4.46 \%, \mathrm{~N}-20.68 \%$ with no solvent of crystallization.

Preliminary oscillation and Weissenberg photographs of a crystal showed that it was triclinic. The unit cell parameters ${ }^{15}$ were obtained from precession photographs. These are $a=6.92 \pm 0.02 \AA$, $b=8.83 \pm 0.02 \AA, c=10.57 \pm 0.03 \AA$, $\alpha=65.0 \pm 0.5^{\circ}, \beta=80.8 \pm 0.5^{\circ}, \gamma=81.2 \pm 0.5^{\circ}$; space group $P_{1}$ or $P_{1}^{-}$. The density measured by floation in aqueous zinc bromide, $1.55 \mathrm{gcm}^{-3}$, is in good agreement with the value $1.56 \mathrm{gcm}^{-3}$ calculated for two molecules per unit cell.

The crystallographic axes with respect to the external morphology are shown in Figure 2. A $c^{\prime}$-axis was chosen normal to the large face (001) and a $b^{\prime}$-axis was chosen normal to the $a c^{\prime}$ plane. This


FIGURE 2 Orientation of the crystallographic axes with respect to the external morphology for a single crystal of the nickel complex.
provides an orthogonal axis system for EPR data collection.

Well resolved spectra were observed in the $a b^{\prime}$ and $a c^{\prime}$ planes while in the $b^{\prime} c^{\prime}$ plane severe overlapping of the superhyperfine lines as well as line broadening due to the pyrrole protons prevented a detailed analysis. The value for $g_{z}$ as determined from the powdered crystal spectra was observed in the $a c^{\prime}$ plane. The maximum value for the copper hyperfine splitting, $A_{z}^{\mathrm{Cu}}$, was observed when the field was parallel to the $g_{z}$ direction.

## ANALYSIS

The magnetic parameters and the direction cosines were determined by the method outlined in the appendix. These values are collected in Tables I and II.

TABLE I
The Magnetic parameters

```
\(g_{z}=2.168 \pm 0.001\)
\(g_{x}=2.042 \pm 0.002\)
\(g_{y}=2.043 \pm 0.002\)
\(A_{z}^{\mathrm{Cu}}=195.1 \pm 0.5 \mathrm{G}\)
    \(197.5 \times 10^{-4} \mathrm{~cm}^{-1}\)
\(A_{x}^{\mathrm{Cu}}=29.9 \pm 1.0 \mathrm{G}\)
    \(28.5 \times 10^{-4} \mathrm{~cm}^{-1}\)
\(A_{y}^{\mathrm{Cu}}=28.6 \pm 1.0 \mathrm{G}\)
    \(27.3 \times 10^{-4} \mathrm{~cm}^{-1}\)
imine, \(A_{z}^{N}=13.9 \pm 0.5 \mathrm{G}\)
            \(14.1 \times 10^{-4} \mathrm{~cm}^{-1}\)
pyrrole, \(A_{z}^{N}=17.5 \pm 0.5 \mathrm{G}\)
            \(17.7 \times 10^{-4} \mathrm{~cm}^{-1}\)
imine, pyrrole, \(A_{x}^{N}=A_{y}^{N}=\begin{aligned} & 15.3 \pm 0.5 \mathrm{G} \\ & 14.6 \times 10^{-4} \mathrm{~cm}^{-1}\end{aligned}\)
methine, \(A_{z}^{H}=6.9 \pm 0.5 \mathrm{G}\)
        \(7.0 \times 10^{-4} \mathrm{~cm}^{-1}\)
\(A_{x}^{H}=A_{y}^{H}=8.6 \pm 0.5 \mathrm{G}\)
    \(8.2 \times 10^{-4} \mathrm{~cm}^{-1}\)
```

TABLE II
Direction cosines of the $g$ values with respect to the laboratory axes.

|  | $a$ | $b^{\prime}$ | $c^{\prime}$ |
| :--- | :--- | :--- | :---: |
| $g_{x}$ | 0.25 | 0 | 0.97 |
| $g_{y}$ | 0 | 1 | 0 |
| $g_{z}$ | 0.97 | 0 | -0.25 |

The superhyperfine splitting along $g_{z}$ consisted of 27 partially overlapped lines. This splitting pattern was first thought to arise from four equivalent nitrogens and the two methine protons since these protons have been known to cause superhyperfine structure in the spectrum of similiar complexes. The spectrum did not yield to such a simple analysis because the lines were unequally spaced. A computer simulation of spectra using different coupling constants for the imine and pyrrole nitrogens accounted for positions of 25 of the 27 lines but the calculated intensities were in poor comparison. Ultimately, a simulation using different nitrogen coupling constants and a methine proton coupling constant of one-half the imine nitrogen value accounted for the missing lines as well as the intensity distribution.

In the molecular plane the superhyperfine structure consisted of nineteen equally spaced lines. This could arise from four equivalent nitrogens and two equivalent protons with a coupling constant of one-half the nitrogen value. Again, the calculated line positions were in agreement but the calculated and experimental intensity ratios were in poor agreement. The observed "extra" lines arising from the protons had intensity ratios less than one-half the expected value. The observed line positions and intensities could be reproduced assuming four equivalent nitrogens and a proton coupling constant of $\left(A_{N}\right)_{/ 2} \pm 1 G$.

In each case, the final simulated spectrum reproduced the observed line positions to within one gauss. The intensities were in good agreement but overlapping prevented an exact comparison.

## BONDING

The molecular geometry of the complex is shown in Figure 2. Assuming $C_{2 v}^{(x)}$ point symmetry, the molecular orbital containing the unpaired electron is the antibonding linear combination of the $d_{x y}$ orbital on the copper with ligand sigma orbitals:

$$
\begin{equation*}
\left.\psi_{B_{2}}=\alpha|x y\rangle-\alpha^{\prime}|2| B_{2}\right\rangle \tag{1}
\end{equation*}
$$

The two coefficients are related by the normalization condition

$$
\begin{equation*}
\alpha^{2}+\alpha^{\prime 2}-2 \alpha \alpha^{\prime} S=1 \tag{2}
\end{equation*}
$$

where $S$ is the overlap integral represented by $2\left\langle x y \mid B_{2}\right\rangle$. Here $\left|B_{2}\right\rangle$ is a ligand group orbital given by

$$
\begin{align*}
\left|B_{2}\right\rangle & =\left|\sum_{i=1}^{4} c_{i} \sigma_{i}\right\rangle \quad c_{i}= \pm 1  \tag{3}\\
\sigma_{i} & =n(2 p)_{i} \pm\left(1-n^{2}\right)^{1 / 2}(2 s)_{i} \tag{4}
\end{align*}
$$

Complete expressions are available for the ligand hyperfine interaction but we shall deal with only the isotropic part, $1 / 3\left(A_{x}^{N}+A_{y}^{N}+A_{z}^{N}\right)$, since correcting for the dipole-dipole contribution requires a knowledge of the copper-nitrogen bond distances and the use of the anisotropic part introduces a large amount of experimental error into the analysis. The isotropic contact term is

$$
\begin{equation*}
A_{\text {iso }}^{N}=4 / 3 \pi \gamma_{N} B_{0} B_{N} \alpha^{\prime 2}\left(1-n^{2}\right)\left|\psi_{2} s(\mathrm{o})\right|^{2} \tag{5}
\end{equation*}
$$

where $\left|\psi_{2} s(0)\right|^{2}$ is the value of the nitrogen $2 s$ function at the nucleus which is estimated ${ }^{16}$ to be $33.4 \times 10^{24} \mathrm{~cm}^{-3}$.

Using the expression, ${ }^{17}$

$$
\begin{align*}
\alpha^{2}= & 7 / 4\left[\frac{\left|A_{\|}^{\mathrm{Cu}}\right|}{P}-\frac{\left|A_{\text {iso }}^{\mathrm{Cu}}\right|}{P}\right. \\
& \left.+2 / 3 g_{\|}-5 / 21 g_{\perp}-6 / 7\right] \tag{6}
\end{align*}
$$

setting $P=0.036 \mathrm{~cm}^{-1}$ and with the spinHamiltonian parameters we obtain $\alpha^{2}=0.728$. If it is assumed that the copper nitrogen bond distances are $1.95 \AA$ and that the hybridization of the nitrogen bonding orbitals is $s p^{2}$ then $S=0.088^{18}$. The normalization condition then gives $\alpha^{\prime 2}=0.362$. Using equation (5) and setting $n^{2}=0.667$ we calculate $A_{\text {iso }}^{N}=16.0 \times 10^{-4} \mathrm{~cm}^{-1}$, in good agreement with the pyrrole value. The smaller observed isotropic splitting for the imine nitrogens could be due to a p :s ratio on the nitrogen greater than two and/or a copper nitrogen distance greater than $1.95 \AA$. Since the overlap integral is a function of both the bond distance and the hybridization we hesitate to calculate a coupling constant without knowledge of the bond distance.

The fractional is electron hole associated with the methine protons is obtained from

$$
\begin{equation*}
p_{H}=\frac{A_{\mathrm{iso}}^{H}}{a_{\mathrm{H}}} \tag{7}
\end{equation*}
$$

where $a_{H}$ is the hyperfine splitting constant for the
hydrogen atom. Using the value ${ }^{19} a_{H}=0.0474 \mathrm{~cm}^{-1}$ and obtaining $A_{\text {iso }}^{H}$ using $\left(A_{N}\right)_{/ 2}+1 G$ as the in-plane methine proton splitting, a value of 0.017 is found. This choice for in-plane proton splitting leads to a ratio of $P_{H}$ in this complex to the value found for $\mathrm{Cu}\left[\mathrm{en}(\mathrm{sal})_{2}\right]^{20}$ of 1.13 . This is the same as the ratio of $\alpha^{\prime 2}$ for the two complexes.

## DISCUSSION

If the crystallographic space group is $P_{1}^{-}$, crystallographic symmetry would demand the occurrence of one magnetic site since the two molecules in the unit cell would be related by an inversion center. This assumption has been critical to the analysis of the superhyperfine splitting. The possibility that the complex superhyperfine pattern partially arises from slightly inequivalent magnetic sites has not been considered. The occurrence of the space group $P_{1}$ in a crystal of this chelate seems unlikely and the good agreement between the observed a nd calculated spectra is good indication that it does not occur here.

The $d_{x y}$ orbital transforms in the molecular point group $C_{2 v}^{(x)}$ as the irreducible representation $B_{2}$ while the $\tilde{d}_{x^{2}-y^{2}}$ and the $d_{z^{2}}$ orbitals transform as $A_{1}$. In $\stackrel{t}{4}$ is type of copper complex in-plane g-anisotropy is expected to be small, due mainly to the difference in energies of the $d_{x z \rightarrow} d_{x y}$ and the $d_{y z \rightarrow} d_{x y}$ transitions. ${ }^{22}$ Accordingly, the amount of rhombic character in the g-tensor in our previous studies ${ }^{13,20,21}$ of tetradentate complexes of the cis " $\mathrm{N}_{2} \mathrm{O}_{2}$ " type has been found to be small, usually within experimental uncertainty. We therefore expect that we have lost no pertinent information by collecting data in only two planes for the system reported in this study.

The $g$-values and copper hyperfine splitting values found for this complex are similar to those observed in copper pthalocyanin ${ }^{23}$ and copper porphyrins ${ }^{24}$. The imino nitrogen splitting values are similar to those obtained in our previous studies on the cis " $\mathrm{N}_{2} \mathrm{O}_{2}$ " complexes while the pyrrole nitrogen values are reminiscent of those found for copper pthalocyanin. ${ }^{25}$

It is interesting to note that the smaller value of $g_{z}$ reported ${ }^{8}$ for $\mathrm{N}, \mathrm{N}^{\prime}$-bis-(o-aminobenzaldehyde) ethylenediimino $\mathrm{Cu}(\mathrm{II})$ should be indicative of greater covalency in that compound. The use of equation (6) and the magnetic parameters give $\alpha^{2}=0.747$ implying less covalency in that compound.

As previously observed, ${ }^{21}\left|A^{\mathrm{Cu}}\right|$ increases with greater covalency rather than decreasing as expected.

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## APPENDIX

The data from each of the two planes was fit to the usual equation via a least square analysis.

$$
\begin{equation*}
\boldsymbol{g}_{e}^{2}=\alpha_{i}+\beta_{i} \cos 2 \theta+\gamma_{i} \sin 2 \theta \tag{8}
\end{equation*}
$$

Here $i$ is the axis of rotation and $\theta$ is the rotation angle, not necessarily the angle the magnetic field makes with an axis in the plane. If we take the $x z$ plane to be a principal plane and the $x y$ plane to be another plane of rotation, it follows that $g_{x y}^{2}=g_{y z}^{2}=0$ and the remaining $g$-tensor elements are given by

$$
\begin{align*}
& g_{x x}^{2}=\alpha_{z}+\left|\left(\beta_{z}^{2}+\gamma_{z}^{2}\right)^{1 / 2}\right| \\
& g_{y y}^{2}=\alpha_{z}-\left|\left(\beta_{z}^{2}+\gamma_{z}^{2}\right)^{1 / 2}\right|  \tag{9}\\
& g_{z z}^{2}=2 \alpha_{y}-\alpha_{z}-\left|\left(\beta_{z}^{2}+\gamma_{z}^{2}\right)^{1 / 2}\right| \\
& g_{x z}^{2}=\left[\beta_{y}^{2}+\gamma_{y}^{2}-1 / 4\left(g_{z z}^{2}-g_{x x}^{2}\right)^{2}\right]^{1 / 2}
\end{align*}
$$

The sign of $g_{x z}^{2}$ is positive if $g_{e}^{2}$ reaches a maximum between the $x$ and $z$ axes and negative if it reaches a minimum. Our $\alpha, \beta$ and $\gamma$ 's relate to Billings and Hathaway's ${ }^{14} a, b$ and $c$ 's as follows: $\alpha=a / 2, \beta=b$, and $\gamma=c$. We have chosen this convention because a fit of the experimental data to equation (8) gives $\alpha=1 / 2(A+B)$ and not $A+B$. Using this convention equations (2) of reference 14 appear without the $1 / 2$ and equations (3) without the $1 / 4$.

If $x z$ is indeed a principal plane, then the three $g$-values and their directions are determined. It is possible for the $g$-tensor to be rhombic with only $g_{z}$ lying in the $x z$ plane. For this case, the average of the two in-plane $g$-values determined by this method will be the same as the average of the actual two-plane $g$-values $\left(g_{\perp}\right)$. No information would be lost in determining bonding parameters since the usual expressions require only $g_{1}$. If the $g$-tensor is axially symmetric then each in-plane $g$-value will still have associated with them a specific direction. Upon diagonalizing the $g$-tensor, the direction obtained for $g_{x}$ is where the coordination plane intersects the $x z$ plane and $g_{y}$ is taken to lie along the $y$-axis.

Since $g_{x y}^{2}=0$ the expression for the angle of misalignment ${ }^{25}$ in the $x y$ plane simplifies to

$$
\begin{equation*}
\delta \theta_{z}= \pm 1 / 2 \arctan \left|\gamma_{z} / \beta_{z}\right| \tag{10}
\end{equation*}
$$

The angle of misalignment in the $x z$ plane can be determined from

$$
\begin{align*}
\delta \theta_{y}= \pm 1 / 2[\arccos & \left|\frac{\left(g_{z z}^{2}-g_{x x}^{2}\right)}{2\left(\beta_{y}^{2}+\gamma_{y}^{2}\right)^{1 / 2}}\right| \\
& \left.\quad-\arctan \left|\gamma_{y} / \beta_{y}\right|\right] \tag{11}
\end{align*}
$$

where the signs are those of $\gamma / \beta$.


[^0]:    $\dagger$ Supported in part by Bureau of Mines, Department of Interior under Contract P0160064.

